

SLIDE 61-62

Calculate partial derivatives of θ

Recall rules: (1) $\frac{\partial}{\partial x} \left(\frac{f}{g} \right) = \frac{f'g - g'f}{g^2}$

(2) $\frac{\partial f(g(x))}{\partial x} = f'g'$

$$\theta = \frac{\bar{R}_P - R_f}{\sigma_P} = \frac{X_A \bar{R}_A + X_B \bar{R}_B - R_f (X_A + X_B)}{(X_A^2 \sigma_A^2 + X_B^2 \sigma_B^2 + 2X_A X_B \sigma_{AB})^{1/2}}$$

rule 1 & 2

$$\frac{\partial \theta}{\partial X_A} = \frac{(\bar{R}_A - R_f) \sigma_P - 1/2 (X_A \sigma_A^2 + X_B \sigma_B^2 + 2X_A X_B \sigma_{AB})^{-1/2} (2X_A \sigma_A + 2X_B \sigma_{AB}) (\bar{R}_P - R_f)}{\sigma_P^2}$$

$$= \frac{(\bar{R}_A - R_f) \sigma_P - \frac{1}{2} \sigma_P^{-1} (2X_A \sigma_A + 2X_B \sigma_{AB}) (\bar{R}_P - R_f)}{\sigma_P^2}$$

Let $\frac{\partial \theta}{\partial X_A} = 0$

$$\Rightarrow \frac{(\bar{R}_A - R_f) \sigma_P - \sigma_P^{-1} (X_A \sigma_A^2 + X_B \sigma_{AB}) (\bar{R}_P - R_f)}{\sigma_P^2} = 0$$

$$\Rightarrow (\bar{R}_A - R_f) - \frac{\bar{R}_P - R_f}{\sigma_P^2} (X_A \sigma_A^2 + X_B \sigma_{AB}) = 0$$

Which is the last eqn at the end of slide 62.